

PONDICHERRY UNIVERSITY

DEPARTMENT OF STATISTICS



SYLLABUS FOR M.Sc. STATISTICS (CBCS Pattern) Effective from the Academic Year 2022-2023

PONDICHERRY UNIVERSITY
PUDUCHERRY 605 014

M.Sc. STATISTICS (CBCS - Semester Pattern)

REGULATIONS

Aim of the Course

The Degree of Master of Science in Statistics aims to train the students in the development and applications of Statistical techniques for analyzing data arising in the scientific investigation of problems in various disciplines. It is also proposed to provide first hand practical experience in handling modern statistical software in the analysis of such data.

Eligibility for admission

Candidates for admission to the first year of the M.Sc. (Statistics) degree programme shall be required to have passed the B.Sc. degree examination of any Indian University recognized by the University Grants Commission with Statistics as the main subject or Mathematics as the main subject with Mathematical Statistics as one of the minor subject and a minimum of 55% marks in the main and allied subjects.

Duration of the Course

The course shall be of two years duration spread over four semesters. The maximum duration to complete the course shall not be more than 8 semesters.

Eligibility for admission to Examination

A candidate shall be permitted to appear for the M.Sc. examination in a subject of study only if he/she secures not less than 70% attendance in the subject concerned.

Medium : The medium of instruction shall be English.

Passing Minimum and Weight age of marks

The weight age of marks for Continuous Internal Assessment (CIA) and end semester examinations shall be 40 and 60 respectively. As per the Choice Based Credit System regulations of the Pondicherry University, a student is declared as pass in a given subject he / she secures

- (a) A minimum of 40% marks in end-semester exam and
- (b) A minimum of 50% marks in aggregate when Internal assessment and End-Semester marks are added together

Supplementary Exam

- (a) A failed student who meets the attendance requirement (70%) and has a minimum of 40% in the Internal Assessment marks may be permitted to register for the next End Semester examination in the following semester itself
- (b) Students who have failed due to insufficient attendance and / or less than 40% in the Internal Assessment marks should repeat the course as and when it is offered.

Continuous Internal Assessment

The weightage of 40 marks for Continuous Internal Assessment component shall consist of the following:

- a) Internal Assessment Tests (two) (2 x 15) = 30 marks
 - b) Seminars/Assignments/Presentations/Viva etc. (1 x 10) = 10 marks
- Internal Total = 40 marks

Choice Based Credit System (CBCS)

The M.Sc. Statistics program is offered through a unique CBCS. The salient feature of the CBCS is that the program is offered through credit based courses. Subjects are divided into Hard Core and Soft Core. Hard Core subjects are compulsory. The students have the choice to select from among the list of soft core subjects. Soft core subjects are similar to elective subjects.

A student is expected to complete a minimum of 72 credits within four semesters. Students are assessed and awarded letter grades based on their performances in the respective courses.

M.Sc. (STATISTICS) – COURSE STRUCTURE
(With effect from 2022-23 onwards)

Objectives

The present course is intended to provide a platform for talented students to undergo higher studies in the subject as well as to train them to suit the needs of the society. Apart from teaching core Statistics subjects, the students are also trained to handle real life problems through practical classes. As part of the course, the students are taught some programming languages and also trained in various statistical softwares such as SPSS, R Programming, MINITAB.

Eligibility

B.Sc. degree in Statistics or Mathematics with Mathematical Statistics as a minor subject with a minimum 55% of marks.

Duration of the Course

The course shall be of two years duration spread over four semesters. The maximum duration to complete the course shall not be more than 8 semesters.

Medium

The medium of instruction shall be English.

Choice Based Credit System (CBCS)

The M.Sc. Statistics program is offered through a unique CBCS. The salient feature of the CBCS is that the program is offered through credit based courses. Subjects are divided into Hard Core and Soft Core. Hard Core subjects are compulsory. The students have the choice to select from among the list of soft core subjects. Soft core subjects are similar to elective subjects.

A student is expected to complete a minimum of 72 credits within four semesters. Students are assessed and awarded letter grades based on their performances in the respective courses.

PONDICHERRY UNIVERSITY
CHOICE BASED CREDIT SYSTEM
M.Sc. STATISTICS SYLLABUS
Effective from the Academic Year 2022 – 2023

Semester	Course Code	Title of the Course	Course Type	No. of Credits
First Semester				
I Semester	STAT-411	Linear Algebra & Matrix Theory	Hard Core	4
	STAT-412	Probability Theory	Hard Core	4
	STAT-413	Distribution Theory	Hard Core	4
	STAT-414	Programming in R (Lab Based)	Hard Core	4
	STAT-415 to STAT 417	Any One Soft Core Course among set of three are allowed	Soft Core	3
Second Semester				
II Semester	STAT-421	Theory of Estimation	Hard Core	4
	STAT-422	Sampling Theory	Hard Core	4
	STAT-423	Stochastic Processes	Hard Core	4
	STAT-424	Regression Analysis	Hard Core	4
	STAT-425	Statistical Laboratory - I Based on Stat-421, Stat-422 and Stat-424 (based on Calculator, Excel & R Programming as per suitability)	Hard Core	3
	STAT-426 to STAT 428	Any One Soft Core Course among set of three are allowed	Soft Core	3
Third Semester				
III Semester	STAT-531	Multivariate Statistical Analysis	Hard Core	4
	STAT-532	Testing of Statistical Hypotheses	Hard Core	4
	STAT-533	Linear Models and Design of Experiments	Hard Core	4
	STAT-534	Statistical Laboratory - II Based on Stat-531,Stat-532 and Stat-533 (based on Calculator, Excel & R Programming as per suitability)	Hard Core	3
	STAT-535 to STAT 538	Any Two Soft Core Courses among set of Four are allowed	Soft Core	3
			Soft Core	3
Fourth Semester				
IV Semester	STAT-541 [@]	Project Work & Comprehensive Viva	Soft Core	12
		Any FOUR relevant soft-core courses either within or outside the department	Soft Core	3
	Soft Core		3	
	STAT-542 to STAT 546		Soft Core	3
			Soft Core	3
Total Credits: 72-(Mandatory)				

@ Students can choose either STAT-541 or any FOUR courses from STAT-542 to STAT-546 as soft-core courses in the Final Semester

Soft Cores Courses in 1 st Semester	Soft Cores Courses in 2 nd Semester	Soft Core Courses in 3 rd Semester	Soft Cores Courses in 4 th Semester
STAT-415: Optimization Techniques	STAT-426: Survival Analysis	STAT-535: Reliability Theory	STAT-542: Actuarial Statistics
STAT-416: Statistical Quality Control	STAT-427: Decision Theory	STAT-536: Bayesian Inference	STAT-543: Data Analysis Using Statistical Packages
STAT-417: Econometrics	STAT-428: Biostatistics	STAT-537: Queuing & Inventory Theory	STAT-544: Demographic Techniques
		STAT-538: Statistical Data Mining Methods	STAT-545: Time Series Analysis
			STAT-546: Total Quality Management

STAT411 - LINEAR ALGEBRA AND MATRIX THEORY

CREDITS: 4

Course Objectives: Understand vector spaces, subspaces and change of basis, Understand linear transformations. Need of Generalized inverse and Moore Penrose inverse of the matrix and to understand bilinear form and quadratic form

Course Outcomes: Compute the inverse of rectangular matrix, Find the matrix representation of linear transformations, Understand applications of vector spaces and subspaces

Unit I

Vector Spaces, Sub-spaces, Basis of a vector space – Vector spaces with inner products Gram-Schmidt orthogonalization.

Unit II

Linear transformation (LT) – Properties – Matrix of a linear transformation – Matrix of composite transformation – Matrix of an inverse transformation – Change of basis Orthogonal transformation - Dual space.

Unit III

Linear equations – Solution space and null space – Sylvester's law of nullity – Generalized inverse of a matrix – Moore – Penrose inverse

Unit IV

Eigen values and Eigen vectors of an LT – left Eigen vectors, right Eigen vectors, Diagonalizable LT – Lambda matrix, Composition of lambda matrices, Operator polynomial, Cayley-Hamilton theorem and minimal polynomial for an LT – Eigen values of matrix polynomials.

Unit V

Bilinear forms Canonical reduction – Sylvester's law of inertia-Definitions of quadratic form Lagrange's reduction – Kronecker's reduction Reduction involving the Eigen values of the matrix, Generalized Eigen value problem.

Books for Study

Biswas S. (2012), Text book of Matrix Algebra, Third Edition, PHI Learning Private Limited, New Delhi.

1. Bhattacharya P.B., Jain S.K., Nagpaul S.K. (2012), First Course in Linear Algebra, New Age International (P) Ltd, New Delhi.
2. Parashar B.P. (1989), Linear Algebra, CBS Publishers and Distributors, Delhi.
3. Rao C.R. (2009), Linear Statistical Inference and its Applications, Second Edition, John Wiley and Sons

Books for Reference

1. Friedberg S.H., Insel A.J. and Spence L.E. (2014), Linear Algebra, Pearson Education.
2. Gilbert J. and Gilbert L. (2005), Linear Algebra and Matrix Theory, Academic Press.
3. Lipschutz S. and Lipson M. (2009), Schaum's outlines, Linear Algebra, Fourth Edition, McGraw Hill Company.
4. Rao A.R. and Bhimasankaram P. (2000), Linear Algebra, Hindustan.
5. Searle S.R. and Khuri A.I. (2017), Matrix Algebra useful for Statistics, Second Edition, John Wiley and Sons, New Jersey.
6. Searle S.R. and Gruber MHI (2016), Linear Models, Second Edition, John Wiley and Sons, New Jersey.

Course Objectives: The objective for this course is to learn the theory and methods of probability theory, and be able to apply and communicate them in practice.

Course Outcomes: A student will be able to: Recognize the role of probability theory in the sciences, communicate the ideas and results of probability; Graduate students will also be able to formulate and apply the definitions of convergence in distribution and in probability, formulate scientific problems involving randomness in mathematical terms, and use probability in their careers

Unit I

Algebra of sets - fields and sigma-fields, Inverse function – Measurable function – Probability measure on a sigma field – simple properties - Probability space - Random variables and Random vectors – Induced Probability space – Distribution functions – Decomposition of distribution functions.

Unit II

Expectation and moments – definitions and simple properties – Moment inequalities – Holder, Jensen, Chebyshev, Markov Inequalities– Characteristic function – definition and properties – Inversion formula.

Unit III

Convergence of a sequence of random variables - convergence in distribution, convergence in probability, almost sure convergence and convergence in quadratic mean - Weak convergence of distribution functions – Slutsky theorem - Helly-Bray theorem.

Unit IV

Definition of product space – Fubini's theorem (statement only) - Independence of two events – Independence of classes – Independence of random variables – properties – Borel zero –one law.

Unit V

Law of large numbers - Khintchin's weak law of large numbers, Kolmogorov strong law of large numbers (statement only) – Central Limit Theorem – Lindeberg – Levy theorem, Linderberg – Feller theorem (statement only), Liapounov theorem – Relation between Liapounov and Linderberg – Feller forms – Radon Nikodym theorem and derivative (without proof) – Conditional expectation – definition and simple properties.

Books for Study

1. Bhat, B. R. (2007): Modern Probability Theory, 3rd edition, New Age International Pvt. Ltd.
2. Ash, R.B. (1972): Real Analysis and Probability, Academic Press.
3. Rohatgi, V.K. and Saleh (2002): An Introduction to Probability Theory and Mathematical Statistics, John Wiley

Books for Reference

1. Athreya K B and Lahiri S N (2005): Measure Theory, Hindustan Book Agency.
2. Tucker, H.G. (1967): A Graduate course in Probability, Academic Press.
3. Burill, C.W. (1972): Measure, Integration and Probability, McGraw Hill.
4. Chow, Y.S. and Teicher, H. (1979): Probability Theory, Springer.
5. Loeve, M. (1985). Probability Theory, 3rd edition, Springer..
6. Resnick S.I. (2001): A Probability Path, Birkhauser.
7. Basu A K. and A Bandopadhyay (2012): Measure Theory and Probability, PHI Learning Pvt. Ltd.

Course Objectives: This course is intended to train students in mathematical techniques of constructing various univariate, bivariate and multivariate distributions.

Course Outcomes: Students will learn about the characterizations of univariate, bivariate and multivariate distributions, its applications and theory of order statistics.

Unit I

Brief review of distribution theory, distribution of functions of random variables - Laplace, Cauchy, Inverse Gaussian, Lognormal, Logarithmic series and Power series distributions - Multinomial distribution

Unit II

Bivariate Binomial – Bivariate Poisson – Bivariate Normal- Bivariate Exponential of Marshall and Olkin - Compound, truncated and mixture of distributions, Concept of convolution

Unit III

Multivariate normal distribution (Definition and Concept only) - Sampling distributions: Non-central chi-square, t and F distributions and their properties - Distributions of quadratic forms under normality-independence of quadratic form and a linear form- Cochran's theorem

Unit IV

Order statistics, their distributions and properties- Joint and marginal distributions of order statistics - Distribution of range and mid range - Extreme values and their asymptotic distributions (concepts only)

Unit V

Empirical distribution function and its properties - Kolmogorov-Smirnov distributions -Life time distributions - Exponential and Weibull distributions - Mills ratio -Distributions classified by hazard rate.

Books for Study

1. Mood M., Graybill F.A. and Boes D.C.(2001) : Introduction to the Theory of Statistics, Tata McGraw-Hill, New Delhi.
2. Johnson, N.L,Kotz, S. and Balakrishnan, N. (1994): Continuous Univariate Distributions, Vol.1 &2, Wiley Series in Probability and Statistics.
3. Johnson, N.L , Kemp A.W. & Kotz, S. (1994): Univariate Discrete Distributions, Wiley Series in Probability and Statistics
4. David H. A. and Nagaraja H.N.(2003): Order Statistics, 3/e, John Wiley & Sons.

Books for Reference

1. Rao C. R.,(1973): Linear Statistical Inference and its Applications, Wiley Eastern Ltd, New Delhi.
2. Dudewicz, E.J and Mishra, S.N(1980): Mathematical Statistics, John Wiley, NY.
3. Kocherlakota S and Kocherlakota K(1992): Bivariate Discrete distributions, M. Dekker.
4. Balakrishnan N and Lai C.D.(2009): Continuous Bivariate Distributions, Springer.
5. Rohatgi, V.K. and Saleh (2002): An Introduction to Probability Theory and Mathematical Statistics, John Wiley.
6. Parimal Mukhopadhyay(2006):Mathematical Statistics, 3/e, Books and Allied (P) Ltd, Kolkata.

This course is partly theory and mostly lab oriented. There will be 2 hours of lectures per week and a minimum of 3 hours of lab. (One credit is equal to one hour of lecture or two hours of Lab.)

Course Objectives: This course is intended to train students to get knowledge in performing statistical data analysis using R language.

Course Outcomes: Students will be able to write program in R language for a various data analytic techniques which will help them in getting placed in analytic companies.

Unit I

R language Essentials: Expressions and objects, Assignments, creating vectors, vectorized arithmetic, creating matrices, operations on matrices, lists, data frames – creation, indexing, sorting and conditional selection ; examples.

Unit II

R Programming: conditional statements – if and if else; loops – for, while, do-while; functions – built-in and user defined; Data entry – reading from text file, data editor; examples.

Unit III

Descriptive Statistics and Graphics: Obtaining summary statistics; generating tables; Bar plots, Pie charts, Box plots, Histogram; exercises.

Unit IV

Probability and Distributions: Random sampling and combinatory; obtaining density, cumulative density and quantile values for discrete and continuous distributions; generating samples from discrete and continuous distributions; Plotting density and cumulative density curves; Q-Q plot.

Unit V

Correlation: Pearson, Spearman and Kendall's correlation; Regression – fitting, obtaining residuals and fitted values; one and two sample tests for mean and variance – one way and two way ANOVA.

Books for Study

1. Michael J.Crawley (2007), The R Book, John Wiley and Sons Ltd.
2. Peter Dalgaard (2008), Introductory Statistics with R, 2nd edition, Springer.

Lab Exercises:

1. Operations on vectors and matrices
2. Creating and manipulating data frames.
3. Writing user defined functions for finding arithmetic mean, median, factorial, matrix addition and multiplication.
4. Bar and Pie charts.
5. Box plots for single and multiple groups.
6. Density and cumulative density plots for Binomial, Poisson, Normal and exponential distributions.
7. Checking Normality using Histogram and Q-Q plot.
8. Correlation coefficient – Pearson's, Spearman and Kendall's Tau.
9. Fitting simple linear and multiple linear regressions.
10. One sample and two sample t test.
11. One way and two way ANOVA.

Course objectives: The objective of the course is to learn the basic concepts in estimation theory like consistency, sufficiency, UMVUE and their applications. To study different methods of estimation and their properties.

Course outcomes: Students will gain knowledge about various statistical estimation methods and their applications.

Unit I

Parametric point estimation – properties of estimators – Consistency and its different forms Sufficient condition for consistency- Unbiasedness – sufficient statistics – Factorization theorem – Distributions admitting sufficient statistic – Exponential and Pitman families procedure for finding minimal sufficient statistic.

Unit II

The information measure – Cramer – Rao (CR) inequality – Chapman – Robbins (KCR) inequality (single parameter case only) – Bhattacharya inequality (single parameter case only) – minimum variance bound estimator- Invariant (equivariant) estimators (concepts only)

Unit III

Uniformly minimum variance unbiased estimators (UMVUE)- condition for the existence of UMVUE- Completeness and Bounded completeness- Relation between complete statistic and minimal sufficient statistic- Rao – Blackwell Theorem- Lehmann – Scheffe's theorem.

Unit IV

Methods of estimation – method of moments and its properties – method of maximum likelihood and its properties-Large sample properties of MLE - Method of minimum chi-square and its properties – Methods of least squares

Unit V

Interval estimation – Pivotal method of construction – shortest confidence intervals and their construction (minimum average width) – Construction of shortest confidence intervals in large samples. Decision Theory: Simple problems involving quadratic error loss function – Elementary notions of minimax estimation – Simple illustrations.

Books for Study

1. Rajagopalan M and Dhanavanthan P (2012): Statistical Inference, PHI Learning, New Delhi.
2. Casella, G. and Berger, R.L. (2002):Statistical Inference, Duxubury Process, Belmont, USA.
3. Rohatgi, V.K. (2003): Statistical Inference, Dover Publications, New York.

Books for Reference

1. Lehmann, E.L and Casella G(1998) :Theory of Point Estimation, 2/e, Wiley Eastern Ltd.
2. B.K.Kale and K.Muralidharan (2015), Parametric Inference – An Introduction, Narosa Publishing House
3. Kale, B.K. (1999): A First course on Parametric Inference , Narosa Publishing House.
4. Zacks,S. (1981): Parametric Statistical Inference, John Wiley, NY.
5. Srivastava, Khan and Srivastava (2014), Statistical Inference: Theory of Estimation, PHI, India

Course objectives: The objectives of this course are to teach basic ideas of sampling from an applied perspective and to provide uses in real life problems. To create the knowledge understanding census and sample survey sampling methods and applying them in practice.

Course Outcomes: Recognize the role of sampling theory in the sciences, it helps in learning various probability and non-probability sampling techniques and which experience how to draw a random sample and what amount of sample with respect to population to be drawn. which will be useful to the students and confidence building in taking decision of any object of the real life problems.

Unit I

Preliminaries – Sampling Designs – Simple random sampling– Stratified Random Sampling – Allocation problems – Systematic Sampling Schemes – Linear, Circular, Balanced and Modified systematic sampling methods

Unit II

Probability Proportional to size sampling- Inclusion Probabilities – Horvitz-Thompson estimator – Yates –Grundy Form –Midzuno Sampling design – PPSWOR- Des-Raj's Ordered estimator – Murty's unordered estimators

Unit III

Ratio estimators and their properties in Simple Random Sampling – Ratio estimators in Stratified Random sampling – Regression Estimators, Regression estimators in Stratified Random Sampling – Multivariate Ratio estimators and Multivariate Regression Estimators

Unit IV

Cluster Sampling: Equal cluster sampling – Estimators of mean and variance, optimum cluster size, Unequal cluster sampling – Estimators of mean and variance – Two stage sampling – variance of the estimated mean – Double Sampling for stratification and Ratio estimation

Unit V

Randomized response methods – Warner's, Simmon's and Two Stage response methods – Sources of errors in Surveys – Mathematical model for the effects of call-backs and the errors of measurement

Books for Study

1. Cochran, W.G. (1977): Sampling Techniques, 3/e, Wiley Eastern Ltd.,
2. Gupta, A. K. and Kabe D.G, (2011): Theory of Sample Surveys, World Scienific Publishing Co. Pte. Ltd., Singapore
3. Singh, D. and Choudhary, F.S (1986): Theory and Analysis of Sample Survey Designs, Wiley Eastern Ltd.,
4. Sukhatme PV. Etal. (1984): Sampling Theory of Surveys with Applications, Iowa State University Press and ISARI Publications, New Delhi

Books for Reference

1. Desraj and Chandhok P.(1998): Sampling Theory, Narosa Publications, New Delhi
2. Kish, L(1995) : Survey Sampling, John Wiley and Sons.
3. Murthy, M.N (1979): Sampling Theory and Methods, Statistical Publishing Society, Calcutta.

5. Sarjinder Singh (2004): Advanced Sampling – Theory with Applications, Kluwer Publications

STAT 423 – STOCHASTIC PROCESSES

CREDITS: 4

Course Objectives: To understand various Processes of exploring the probability patterns, to understand Random Processes and finding Transition Probabilities, to formulate probability distributions with different types of stochastic processes and to get acquaintance with different applications of stochastic processes.

Course Outcomes: After completion of the course the student can learn about

1. Markov processes and development of transition probability matrices
2. Derivations of probability functions with the approaches of differential equations and Markov chains
3. The processes namely Birth, Death, Poisson, Weiner, Renewal, Branching and Time series Processes.
4. Deriving different statistical characteristics with above mentioned processes.

Unit I

Stochastic processes: Definition and classification – Markov chain– Examples (Random walk, Gambler's ruin problem)- Transition Probability Matrices - Higher Transition Probabilities - Bernoulli Trails - classification of states and chains - theorems and problems; Basic limit theorem of renewal theory.

Unit II

Poisson Process: Overview- postulates- probability mass function -Properties - inter related probability distributions- Generalization- Arrival process, Departure Process, Pure Birth(Yule-Furry) process, Birth and Death Processes, Birth-Death and Migrations processes- Chapman Kolmogorov Equations- Compound Poisson Process - Transition density matrix and Poisson Process.

Unit III

Weiner Process: Brownian Motion, Joint probabilities, Wiener process, Differential equations, Kolmogorov equations, First passage time distribution; Branching Process: properties of generating functions of branching processes, Probability of Ultimate extinction, Distribution of Total number of Progeny, Age dependent Branching process

Unit IV

Renewal processes: Definition, examples and relationships between terms – renewal interval, delayed recurrent event, Renewal Processes in continuous time, Renewal Function and renewal density, renewal equation, renewal theorems – Study of residual life time process

Unit V

Stationary processes and Time Series: Stationary Processes, second order, stationarity, Gaussian Processes, weakly and strongly stationary process; Time Series- White Noise process, first order Markov process, MA and AR processes, Autoregressive process of order two, ARMA process verification of stationarity.

Books for Study

1. Karlin, S and Taylor, H.M(1975): A First Course in Stochastic Processes, Academic Press, New York.
2. Medhi,J (2009): Stochastic Processes, 3/e, New age International.
3. Bhat B.R.(2004): Stochastic Models: Analysis and Applications, New Age Publications

Books for Reference

1. Bhattacharya and Waymire, E.C. (1992): Stochastic Process with Applications John Wiley and sons.
2. Jones,P.W and Smith,P(2001): Stochastic Processes: An Introduction, Arnold Press.
3. Cinlar, E(1975): Introduction to Stochastic Processes, Prentice-Hall Inc., New Jersey.
4. Cox, D.R and Miller, H.D(1983) : Theory of Stochastic Processes – Chapman and Hall, London,Third Edition
5. Ross S.M (1983): Stochastic Process, Wiley.
6. G. Grimmett and D. Stirzaker (2001): Probability and Random Processes, 3/e, OUP Oxford.

STAT 424 REGRESSION ANALYSIS

CREDITS: 4

Course Objectives: This course is intended to train students to get knowledge in theoretical and practical applications of regression techniques.

Course Outcomes: Students will be able to perform predictive analytics for real life problems.

Unit I

Review of Linear Models Full rank linear model – least square estimators of the parameters and their properties – Gauss-Markov theorem – Model in centered form – Estimators under normality assumption and their properties – Coefficient of determination – Generalized least squares – misspecification of the error structure and the model.

Unit II

Test for overall regression and for a subset of the parameters – test in terms of R^2 – General Linear Hypothesis testing – special cases – confidence region for the parameters and the mean – prediction intervals – likelihood ratio tests for the parameters – study of the residual outliers and influential observations

Unit III

Selection of input variables and model selection – Methods of obtaining the best fit – Stepwise regression, Forward selection and backward elimination – Multicollinearity – Collinearity diagnostics – Causes, Consequences and Remedy –Departure from normality

Unit IV

Introduction to general non-linear regression – Least squares in non-linear case – Estimating the parameters of a non-linear system Non-linear growth models – Concept of non-parametric regression

Unit V

Robust regression – Linear absolute deviation regression – M estimators – least squares approach based on M-estimators – Re-sampling procedures for regression models – Bootstrap and Jackknife methods and its properties (without proof).

Books for Study

1. Alvin C. Rencher (2000): Linear Models in Statistics, John Wiley & Sons, New York (Chapters 7,8 & 9 for Unit I & II)
2. Draper, N and Smith, H (1998): Applied Regression Analysis, 3rd Edition, Wiley-Interscience.
3. Elizabeth C. Peck, Douglas C. Montgomery, G. Geoffrey Vinning (2006): Introduction to Linear Regression Analysis, 3/e, John Wiley & Sons.

Books for Reference

1. Chatterjee, S, Ali S. Hadi (2013): Regression Analysis by Example, 5th edition, John Wiley.
2. Searle, S.R. (1997): Linear Models, John Wiley.
3. Thomas P. Ryan (2006): Modern Regression Methods, John Wiley and Sons, Inc.
4. Seber G.A.F and Wild C.J. (2003): Nonlinear Regression, John Wiley & Sons

STAT 425 - STATISTICAL LABORATORY – I

CREDITS: 3

(Based on STAT 421, STAT 422 and STAT 424) (based on Calculator, Excel & R Programming as per suitability)

Course Objectives: This course is intended to train students to get knowledge in practical applications of Estimation Theory, Sampling Theory and Linear models

Course Outcomes: Students will be able to perform analysis of data sets using various statistical software.

I. Estimation (20 marks)

1. MLE and Standard error of ML estimators.
2. MLE through the method of successive approximation.
3. MLE for truncated distribution.
4. Method of Moments
5. Method of Minimum Chi-square
6. Method of Least square
7. Interval estimation: Confidence interval for mean,
8. Interval estimation - difference of means,
9. Interval estimation - variance and ratio of variances.

II. Sampling Theory (20 marks)

1. Simple random sampling methods of drawing sample – Estimation of the population total and variance estimation.
2. PPSWR – Hurwitz Thompson estimator - Des Raj ordered estimator – Murthy's unordered estimator – Midzuno scheme.
3. Linear and circular systematic sampling.
4. Stratified sampling – SRS, PPSWR, PPSWOR
5. Cluster sampling – of equal sizes.
6. Ratio, Regression and Difference estimation estimators.

III Linear Models and Regression Analysis (20 marks)

1. Fitting of Multiple linear regression model
2. Residual Analysis for model adequacy, detection of outliers and influential observations
3. Variable Selection procedures
4. Collinearity Diagnostics

Course Objectives: To learn about multivariate normal distribution and its characterizations. To study the multivariate tests for mean vectors and covariance matrices. To know the theoretical concepts and applications of multivariate statistical methods like Discriminant Analysis, Principal Component Analysis, Canonical Correlation Analysis and Factor Analysis

Course Outcomes: Enable to understand the mathematical framework in multivariate statistical analysis and how to implement them in practical situations.

Unit I

Multivariate normal distribution– Marginal and conditional distributions – characteristic function. Maximum likelihood estimation of the parameters of Multivariate Normal and their sampling distributions – Inference concerning the mean vector when covariance matrix is known

Unit II

Total, Partial, Multiple correlation in the Multivariate setup – MLEs of Total, Partial and Multiple correlation coefficients. Sampling distributions of Total and Multiple Correlation in the null case. Hotelling T^2 statistic, derivation and its distribution –Uses of T^2 statistic - relation between T^2 and D^2 – Mahalanobis D^2 statistic and its distribution

Unit III

Generalized variance – Wishart distribution (statement only) – Properties of Wishart distribution – Test for covariance matrix – Test for equality of covariance matrices

Unit IV

Classification problems – Classification into one of two populations (known and unknown dispersion matrix) – Classification in to one of several populations – Fisher's Linear discriminant function

Unit V

Principal components –properties, Extraction of Principal components and their variances Canonical correlation – Estimation of canonical correlation and variates. Factor analysis – Mathematical model- Estimation of Factor Loadings — Concept of factor rotation – Varimax criterion

Books for Study

1. Anderson, T.W. (2003) : An Introduction to Multivariate Statistical Analysis, Wiley Eastern Ltd.
2. Johnson, R. A and. Wichern D.W (2007): Applied Multivariate Statistical Analysis, 6 /e, Prentice-Hall of India Private Ltd., New Delhi.
- Giri, N.C(2003): Multivariate Statistical Inference, Academic Press, NY

Books for Reference

1. Morrison, F(1985): Multivariate Statistical Methods, Mc Graw Hill Book Company.
2. Rao, C.R(1998): Linear Statistical Inference and its Applications, Wiley Eastern Ltd.,
3. Alvin C. Rencher(2002): Methods of Multivariate Analysis, 2/e, Wiley Interscience
4. Srivastava M.S. and Khatri C.G.(1979):Introduction to Multivariate Analysis, Elsevier

Course Objectives: To emphasize on the theoretical concepts of testing single and composite hypotheses under parametric and non-parametric set up.

Course Outcomes: Enable to understand the mathematical framework in testing problems and how to implement them in practical situations.

Unit I

Randomized and non-randomized tests, Neyman – Pearson fundamental lemma, Most powerful tests, Uniformly most powerful test, Uniformly most powerful test for distributions with monotone likelihood ratio, Generalization of fundamental lemma and its applications

Unit II

Unbiasedness for hypothesis testing, Uniformly most powerful unbiased tests, Unbiased tests for one parameter exponential family, Similar test and complete sufficient statistics, Similar tests with Neyman structure, Locally most powerful tests.

Unit III

Invariant tests, maximal invariants, Uniformly most powerful invariant tests, Consistent tests, Likelihood ratio test, its properties and its asymptotic distribution, Applications of the LR method.

Unit IV

Non-parametric tests: Goodness of fit test : Chi-square and Kolmogorov Smirnov test - Test for randomness, Wilcoxon Signed rank test – Two sample problem: Kolmogorov-Smirnov test, Wald-Wolfowitz run test, Mann-Whitney U test, Median test, Kruskal Wallis test and Friedman's test

Unit V

Sequential tests: Basic Structure of Sequential tests – Sequential Probability Ratio Test (SPRT) and its applications – Determination of the boundary constants – Operating Characteristic and expected sample size of SPRT – Optimum properties of SPRT.

Books for Study

1. Rajagopalan M and Dhanavanthan P (2012): Statistical Inference, PHI Learning, New Delhi.
2. Lehmann, E.L and Joseph P. Romano (2005): Testing Statistical Hypotheses, 3/e, Springer
3. Rohatgi, V.K.(2003): Statistical Inference, Dover Publications,.
4. Gibbons, J.D. (1985) : Non Parametric Statistical Inference , 2/e , Marcel Dekker.

Books for Reference

1. Casella, G & Berger, R.L (1990):Statistical Inference , Duxbury Press, Belmont. USA
2. Ghosh,B.K(1970): Sequential Tests of Statistical Hypotheses, Addison Wesley.
3. Parimal Mukhopadhyay(2006):Mathematical Statistics, 3/e, Books and Allied (P) Ltd, Kolkata.
4. Manoj Kumar Srivastava and Namita Srivastava (2009): Statistical Inference – Testing of Hypotheses, Prentice Hall of India

Course Objectives: Understand the need of experimental design, understand the link between linear models and design of experiments, Understand the principles of Design of experiments, Understand different design of experiments.

Course Outcomes:

- (1) Able to do understand the logic behind a particular design.
- (2) Formulation of specific design in mathematical form.

Unit I

Full rank linear model – least square estimators of the parameters and their properties – Gauss-Markov theorem – Model in centered form – Estimators under normality assumption and their properties – Coefficient of determination – Generalized least squares – misspecification of the error structure and the model.

Unit II

Notion of design matrix- general analysis of design models (Inter and Intra Block analysis) – C Matrix and its properties – Expected Mean Squares (EMS) and its uses- Algorithm for calculating EMS – Two way elimination of heterogeneity – Orthogonality – Connectedness and resolvability

Unit III

Principles of scientific experimentation – Basic Designs: Overview of Completely Randomized Design (CRD), Randomized Block Design (RBD) and Latin Square Design (LSD) – Analysis of RBD (with one observation per cell, more than one but equal number of observations per cell) – Derivation of one and two missing values: Iterative and non-iterative methods – Loss of Efficiency due to missing values- Multiple comparison test: Least Significant Difference, Student Newman Kuel , Duncan's Multiple Range, Tukey tests.

Unit IV

Balanced Incomplete Block Design (BIBD)– Types of BIBD – Simple construction methods – Concept of connectedness and balancing – Intra Block analysis of BIBD – Recovery of Inter Block information – Partially Balanced Incomplete Block Design with two associate classes – intra block analysis only - Split plot and strip plot design and their analysis.

Unit V

Factorial experiments: 2^2 , 2^3 , 2^4 and 3^2 , 3^3 experiments and their analysis – Complete and Partial Confounding - Fractional Replication in Factorial Experiments

Books for Study

1. Das, M.N. and Giri, N.C(1979): Design and Analysis of Experiments, Wiley Eastern Ltd,
2. Douglas C. Montgomery (2009) : Design and Analysis of Experiments, 7/e, John Wiley and Sons,
3. Graybill, F.A(1961) : An Introduction to Linear Statistical Models, Mc Graw Hill Book Company

Books for Reference

1. John, P.W.M (1971): Statistical Design and Analysis of Experiments, Mc Graw Hill Book Company.
2. Kempthorne, O(1966): The Design and Analysis of Experiments, John Wiley and Sons.

3. Ragahavarao, D(1971): Constructions and Combinatorial Problems in Design of Experiments, John Wiley and Sons.
4. Searle, S.R(1987) : Linear Models, John Wiley and Sons.
5. Cochran .W.G. and Cox .G.M. (1995): Experimental designs, 4/e, Wiley.
6. Cobb G.W.(1998): Introduction to Design and Analysis of Experiments.
7. Parimal Mukhopadhyay(2005):Applied Statistics, 2/e, Books and Allied (P) Ltd, Kolkata.
8. R. Paneerselvam (2012), Design and Analysis Experiments, PHI Learning Pvt. Ltd
9. K.Krishnaiah and P. Shahabudeen (2013), Applied Design of Experiments and Taguchi Mehtods, PHI Learning Pvt. Ltd.

STAT 534 – STATISTICAL LABORATORY – II

CREDITS: 3

(Based on STAT 531, STAT 532 and STAT 533)

(based on Calculator, Excel & R Programming as per suitability)

Course Objectives: This course is intended to train students to get knowledge in practical applications of Hypothesis testing, Multivariate analysis and Design of experiments.

Course Outcomes: Students will be able to perform analysis of data sets using various statistical software.

I Testing of Hypotheses

(20 marks)

1. Construction of randomized and nonrandomized MP, UMP and UMPU tests of hypotheses and drawing the power curves.
2. Construction of SPRT and its OC and ASN curves.
3. Non parametric tests:
Kolmogorov Smirnov test, Mann-Whitney U test, Median test for k-sample problem, Kruskal Wallis test and Friedman's test

II Multivariate Statistical Analysis

1. Test for equality of mean vectors when covariance matrix is unknown (Hotelling's T^2 test)
2. Test for Two Covariance matrices
3. Discriminant Analysis
4. Canonical correlation and canonical variables
5. One Way MANOVA with Post hoc tests (DMRT and Tukey's).
6. Principal Component Analysis
7. Factor Analysis

III Design of Experiments (20 marks)

1. Multiple Comparison tests (Least Significant Difference (LSD) test, Bonferonni's test)
2. Missing Data Analysis- one and two observations in RBD
3. Missing Data Analysis- one and two observations in LSD
4. 2^4 , 3^2 factorial experiments
5. Fractional factorial experiments
6. Complete confounding in 2^4 , 3^2 factorial experiments
7. Partial confounding in 2^4 , 3^2 factorial experiments
8. Split plot design
9. BIBD
10. Youden Square Design
11. Analysis of Covariance – CRD – One Concomitant Variable
12. Analysis of Covariance – RBD – One Concomitant Variable

SOFT CORE PAPERS

SEMESTER I

STAT 415 – OPTIMIZATION TECHNIQUES

CREDITS: 3

Course Objectives:

1. To understand various issues of optimizations techniques linked with Mathematical Programming
2. To solve the Linear and Non linear programming formulae by using different methods
3. To learn about post optimality and sensitivity analysis with different optimization techniques
4. To pursue classical aspects with mathematical concepts and empirical procedures with numerical Illustrations

Course Outcomes:

After completion of the course the student can learn about

1. Formulation and solving procedures with graphical method, simplex method with and without artificial variables, duality of LPP, dual simplex method, revised simplex method.
2. Conducting Post optimality sensitivity analysis, solving Integer LPP with branch and bound, Montgomery Cut plane methods.
3. Solving procedures of Dynamic Programming techniques with Bellman's Principle, LPP, Manpower allocation, Travel salesman routing problem, Resources allocation etc.
4. Solving procedures for Network scheduling, Probability computations for PERT, cost Optimality analysis with CPM

Unit I

Mathematical Programming - Solving of LPP by graphical method - Linear Programming Problem (LPP)–Simplex, Big M and Two Phase methods – Revised simplex method – Solving LPP using Duality - Dual Simplex method

Unit-II

Post Optimality and Sensitivity Analysis–Variation in cost vector and requirement vector– Addition and deletion of single variable and single constraint - Integer Programming Problem (IPP) - Gomory's cutting plane algorithm– Mixed IPP – Branch and Bound technique

Unit III

Dynamic programming problem (DPP) - Bellman's principle of optimality - General formulation - computation methods and application of DPP - Solving LPP through DPP approach

Unit IV

Non Linear Programming: Constrained and Unconstrained Problems of Maxima and minima, Constraints in the form of equations (Lagrangian Method) and in equations (Kuhn-Tucker conditions), Quadratic programming: Beale's and wolf's methods simplex method for quadratic programming.

Unit- V

PERT - CPM: Applications, Basic Steps in PERT/CPM techniques; Time estimates and Critical Path in Network Analysis; Optimum and minimum duration cost, PERT, Resource Allocations.

Text Books

1. Hillier FS and LibermannGJ(2002):IntroductiontoOperationsResearch,7th Edition, McGraw Hill
2. KantiSwarup,P.K.GuptaandManMohan(2004):OperationsResearch,SultanChand and

Sons, New Delhi.

3. Gross D, Shortle J.F. , Thompson J.M. and Harris C.M. (2011): Fundamentals of Queuing Theory, John Wiley & Sons

Reference Books

1. Sinha SM(2006):Mathematical Programming: Theory and Methods, Elsevier Publications.
2. Devi Prasad (2015), Operations Research, Narosa Publishing House
3. Kapoor V.K.(2008):Operations Research, 8/e,SultanChand&Sons
4. Sharma .S.D(1999): Operation Research , Kedar Nath RamNath & Co., Meerut.
5. Hamdy A.Taha(1987):Operations Research – An Introduction, 4/e, Prentice Hall of India, PrivateLtd,NewDelhi.
6. Sujit K. Bose (2012), Operations Research Methods, 2/e, Narosa Publishing House
7. K. Chandrasekhara Rao and Shanti Lata Misra (2012), Operations Research, Narosa Publishing House

Course Objectives: To give exposure on the practical implementation of the quality control techniques and acceptance sampling schemes.

Course Outcomes: Students will be able to cater the needs of the industry to resolve the quality issues.

Unit I

Modified control charts for mean – CUSUM chart – technique of V-mask – Weighted Moving average charts – multivariate control charts – Hotelling's T^2 control charts and Economic design of X-bar chart

Unit II

Process Capability analysis: Meaning, Estimation technique for capability of a process – Capability Indices: Process capability ratios C_p , C_{pk} , C_{pm} , C_{mk} , C_{pc} – Process capability analysis using a control chart – Process capability analysis using design of experiments

Unit III

Acceptance sampling – Terminologies – Attribute sampling plan by attributes – Single sampling plan and Double sampling plan – OC, ASN, AOQ, AOQL and ATI curves – MILSTD -105E Tables

Unit IV

Acceptance sampling variables for process parameter – Sequential plans for process parameter (σ known and unknown) – Sampling variables for proportion non-conforming - \bar{X} method, K method –

Unit V

Double specification limits – M-method, Double sampling by variables - MILSTD -414 Tables – Continuous Sampling plan – CSP-1, CSP-2, CSP-3, Wald and Wolfowitz SP-A and SP- B

Text Books

1. Douglas C. Montgomery (2009): Introduction to Statistical Quality Control, 6/e, John Wiley and Sons, New York.
2. Edward G. Schilling, Dean V. Neubauer, (2009), Acceptance Sampling in Quality Control, Second Edition, Taylor & Francis
3. Oakland, J.S.(1989): "Total Quality Management", Butterworth-Hcinemann Ltd., Oxford

Reference Books

1. Mittage, H.J and Rinne, H(1993): Statistical Methods of Quality Assurance, Chapman Hall, London, UK
2. Zeiri (1991): "Total Quality Management for Engineers", Wood Head Publishers.
3. Juran J.M and Frank M.Gryna Jr .(1982): "Quality Planning and Analysis", TMH, India.

Course objectives: This course provides insight knowledge about Econometrics, Econometric modeling, its application with real time data and as an outcome it is used for researchers and in areas such as Statistics, Economics and Finance.

Course outcomes: Students will be able to apply various econometric models to address the issues concerning economic and longitudinal data.

Unit I

Nature and Scope of Econometrics - Review of General Linear Model (GLM), Ordinary Least Squares (OLS), Generalized Least Squares (GLS) and Multicollinearity – Sources, consequences and detection – Principal Component regression and Ridge Regression.

Unit II

Heteroscedasticity - consequences and detection: Graphical methods – Tests: Park test – Glejser's test – Spearman's rank Correlation test – Goldfeld-Quandt test – Breusch-Godfrey-Godfrey test and White's General Heteroscedasticity test – remedial measures for Heteroscedasticity – Weighted Least Squares approach.

Unit III

Linear regression with stochastic regressors - Errors in variables - Instrumental variable estimation - Autocorrelation – consequences and tests: Run's test –Durbin-Watson test - Autoregressive linear regression

Unit IV

Distributed lag models – Finite and Infinite Distributed lag models – Koyck's approach, Almons' Model, Cagan's approach, Arithmetic Lag, Geometric Lag model, Inverted V Lag Model, Pascal's Lag Model, Nerlove's Lag Model, Instrumental Variable method.

Unit V

Simultaneous linear equations model - Identification problem - Restrictions on structural parameters - rank and order conditions - Restrictions on variances and covariances - Estimation in simultaneous equations model

Text Books:

1. Gujarati, D.N. (2003): Basic Econometrics, McGraw Hill.
2. Johnston, J. (1984): Econometric methods, Third edition, McGraw Hill.
3. Nachane. D.M. (2006): Econometrics: Theoretical Foundations and Empirical Perspective, Oxford University Press.

Reference Books:

1. Apte, P.G. (1990): Text book of Econometrics. Tata McGraw Hill.
2. Intrulligator, M.D. (1980): Econometric models - Techniques and Applications, Prentice Hall of India.
3. Kleiber, C. and Zeileis, A. (2008): Applied Econometrics with R, Springer, NY.

SEMESTER – II

STAT 426 - SURVIVAL ANALYSIS

CREDITS: 3

Course Objectives: To aware about the dealing of life time data in engineering and medical sciences, to learn several methods in reliability theory as well as survival analysis, apply these techniques to prevent or to reduce the likelihood or frequency of failures.

Course Outcomes: To predict the life time of subject and to know the pattern of rate of failure and compare the treatments in medical sciences.

Unit I

Concepts of time, Order and random Censoring, likelihood in these cases. Life distributions- Exponential, Gamma, Weibull , Lognormal , Pareto , Linear Failure rate. Parametric inference (Point estimation, scores, MLE)

Unit II

Life tables, failure rate, mean residual life and their elementary properties. Concept of Ageing, Types of Ageing classes and their properties and relationship between them , Bathtub Failure rate, Concept of Inverse Hazard rate.

Unit III

Estimation of survival function Actuarial Estimator, Kaplan- Meier Estimator, Estimation under the assumption of IFR / DFR . Tests of exponentiality against non- parametric classes- Total time on test, Despane test.

Unit IV

Two sample problem- Gehan test, Log rank test. Mantel Haenszel test, Tarone Ware tests. Introduction to Semi- parametric regression for failure rate, Cox's proportional hazards(PH) model with one and several covariates and estimation problems in Cox's PH Model. Rank test for the regression coefficients.

Unit V

Introduction to Competing risks analysis and estimation problems in competing risk model for parametric and non- parametric semi parametric set up. Ideas of Multiple decrement life table and its applications.

Books for Study:

1. Miller, R.G. (1981) : Survival analysis (John Wiley).
2. Cox, D.R. and Oakes, D. (1984) : Analysis of Survival Data, Chapman and Hall, NewYork.
3. Elisha T Lee, John Wenyu Wang and Timothy Wenyu Patt(2003): Statistical Methods for Survival data Analysis, 3/e, Wiley Inter Science.

Books for Reference:

1. Gross, A.J. and Clark, V.A. (1975) : Survival distribution : Reliability applications in the Biomedical Sciences, John Wiley and Sons.
2. Elandt Johnson, R.E. Johnson N.L.: Survival Models and Data Analysis, John Wiley and sons.
3. Kalbfleisch J.D. and Prentice R.L.(1980), The Statistical Analysis of Failure Time Data, JohnWiley.
4. Klelin P. John and Moeschberger(2003): Survival Analysis: Techniques for Censored andTruncated Data, 2/e, Springer.
5. Lawless J.F. (1982) Statistical Models and Methods of Life Time Data; John Wiley & Sons.

Unit I

Basic elements of a decision problem - Randomized and non-randomized decision rules - Estimation and testing of hypothesis as decision problems - Baye's approach to inference and decision -

Unit II

Loss functions - Prior and Posterior distributions and its analysis for Bernoulli, Poisson, and normal processes - Decision principles and Baye's risk–

Unit III

Utility theory - axioms, construction of utility functions, sufficiency, equivalence of classical and Bayesian sufficiency, complete and essentially complete classes of decision rules

Unit IV

Minimax analysis - Basic elements of game theory - General techniques of solving games - Finite games - Supporting and separating hyper plane theorems - Minimax theorem - Minimax estimation for normal and Poisson means

UNIT V

Admissibility of Baye's and minimax rules, General theorems on admissibility, Robustness of Baye's rules, Invariant decision rules, Location parameter problems, Confidence and credible sets.

Text Books:

1. James O. Berger (1980): Statistical Decision Theory and Bayesian Analysis, Springer Verlag
2. M.H. DeGroot (1970): Optimal Statistical Decisions, John Wiley
3. H. Raiffa and R. Schlaifer (2000): Applied Statistical Decision Theory, Wiley

Reference Books:

1. Zellener (1971): An Introduction to Bayesian Inference in Econometrics, Willey
2. Hayes J. G and Winkler R I (1976): Probability, Statistics and Decision, Dower
3. Anthony O' Hangan (1994): Kendall's Advanced theory of Statistics Vol. 2B, Bayesian Inference, John Wiley

Course Objectives: Enable the students to understand the basic preliminaries and advanced modeling techniques applied in biological and medical sciences.

Course Outcomes: This course will enhance the capability in handling practical situations that arise in pharmaceutical and health care industries.

Unit I

Statistical Methods in Clinical Trials: Introduction to clinical trial and its phases I, II, III and IV, statistical designs-fixed sample trials: simple randomized design, stratified randomized crossover design; Sequential design - open and close sequential design. Randomization-Dynamic randomization, Permuted block randomization; Blinding-Single, double and triple.

Unit II

Biological Assays: Introduction, parallel-line assay, slope- ratio assays and quantile- response assay, Feller's theorem. Dose-response relationships-qualitative and quantitative response, dose response relation- estimation of median effective dose – PK-PD Analysis.

Unit III

Categorical Data Analysis: Categorical response data, logistic regression-odds ratio, Wald's statistic, logistic regression and its diagnostics, - Poisson regression – Estimation of relative risk and its applications.

Unit IV

ROC Curve analysis - Estimation of Binomial Model and the Area under the Curve, its applications – Properties of ROC curve - Kullback –Leibler Divergence (KLD)– definition – functional relationship between Kullback –Leibler Divergence and the slope of the ROC curve – derivations of KLD expressions for Bi-normal ROC model

Unit V

Repeated Measures ANOVA – One Way and Two Classified Data –Measures of disease frequency – incidence – prevalence – relative risk – Epidemiological study designs – Cohort study design and its analysis – Case control study design and its analysis – concept of bias – information bias and selection bias

Text Books

1. Elisa T.Lee & John Wenyu Wang (2003): Statistical methods for Survival Data analysis, 3rd Edition, John Wiley
2. Jerrold H. Zar (1999): Biostatistical Analysis, 4th edition, Pearson
3. Armitage, P, Berry G and Mathews J.N.S (2002): Statistical Methods in Medical Research, 4/e, Blackwell Scientific Publications
4. Krzanowski, W and Hand, D.J.(2009): ROC Curves for Continuous Data, Chapman and Hall

Reference Books

1. Hosmer and Lemeshow (2000): "Applied Logistic Regression", 2/e, Wiley Series
2. Alan Agresti (2002): Categorical Data analysis, 2/e, John Wiley
3. Sylvia Wasserthial and Smoller, (2004): Biostatistics and Epidemiology – A Primer for Health and Biomedical professionals, 3rd Edition, Springer
4. Rastogi, V.B. (2006): Fundamentals of Biostatistics, ANE Books, India

SEMESTER III

STAT 535 – RELIABILITY THEORY

CREDITS: 3

Course Objectives: To aware about the dealing of life time data in engineering and medical sciences, to learn several methods in reliability theory as well as survival analysis, apply these techniques to prevent or to reduce the likelihood or frequency of failures.

Course Outcomes: To predict the life time of subject and to know the pattern of rate of failure and compare the treatments in medical sciences.

Unit I

Introduction to Reliability and its needs; Structural properties of coherent system: components and systems, coherent structures, representation of coherent systems in terms of paths and cuts, relevant & irrelevant structure; Modules of coherent systems; Reliability of a coherent systems; Reliability importance of components; Bounds on System Reliability.

Unit II

Life Distributions: Concept of distribution function, hazard function, Reliability function, MTTF, Bathtub failure rate; loss of memory property of Exponential distribution - parametric families of some common life distributions – Exponential, Weibull and Gamma and its characterization - Reliability estimation of parameters in these models.

Unit III

Notions of Ageing; Classes of life distributions and their duals - preservation of life distribution classes for reliability operation - Formation of coherent systems, convolutions and mixtures.

Unit IV

Univariate stock models and life distributions arising out of them: cumulative damage model, shock models leading to univariate IFR, Successive shock model; bivariate shock models; common bivariate exponential distributions due to shock and their properties. Maintenance and replacement policies; availability of repairable systems; modeling of a repairable system by a non-homogeneous Poisson process.

Unit V

Stress-Strength reliability - Concepts and its estimation for exponential, Weibull and gamma distributions; Reliability growth models; probability plotting techniques; Hollander –Proschan and Deshpande tests for exponentiality – Basic ideas of accelerated life testing.

Text Books:

1. Barlow, R.E. and Proschan F. (1985) Statistical Theory of Reliability and Life Testing; Rinehart and Winston.
2. Lawless, J.F. (2003): Statistical Models and Methods of Life Time Data; John Wiley.

Reference Books:

1. Bain L.J. and Max Engelhardt (1991): Statistical Analysis of Reliability and Life Testing Models; Marcel Dekker.
2. Nelson, W (1982): Applied Life Data Analysis; John Wiley.
3. Zacks, S(1992): Introdcution to Reliability Analysis, Springer Verlag.
4. Marshall, A.W. and Olkin I(2007): Life Distributions, Springer

Course Objectives: To learn advance method of estimation. The objectives of the Bayesian inference is that to incorporate the past information with observed data in order to predict the future inferences.

Course Outcomes: The students would able to calculate relative frequencies to estimate probabilities. Calculate conditional probabilities using Bayes's rule. It also helps to incorporate the various types of priors for drawing inference from Posterior distribution

Unit I

Introduction about Thomas Baye's-Motivations and Contributions - Evaluation of Subjective probability of an event using a subjectively unbiased coin - Subjective prior distribution of a parameter – Baye's theorem and computation of the posterior distribution.

Unit II

Introduction of Prior Distributions, Types of Prior Distributions, Proper Prior-Enlarging the natural conjugate family by enlarging hyper parameter space - mixtures from conjugate family - choosing an appropriate member of conjugate prior family - Non informative, improper and invariant priors - Jeffrey's invariant prior

Unit III

Bayesian point estimation: Prediction problem from posterior distribution - Baye's estimators for absolute error loss, squared error loss, linear loss function, Jeffrey's and 0 -1 loss - Generalization to convex loss functions - Evaluation of the estimate in terms of the posterior risk

Unit IV

Bayesian interval estimation : Credible intervals - Highest posterior density regions - Interpretation of the confidence coefficient of an interval.

Unit V

Bayesian Testing of Hypothesis: Prior and Posterior odds - Baye's factor for various types of testing hypothesis problems -Monte-Carlo Integration and Basic Concepts on Markov chain Monte Carlo techniques (MCMC)(without proof).

Text Books

1. Bansal A.K.(2007): Bayesian Parametric Inference, Narosa Publications
2. Sinha S K (1998): Bayesian Estimation, New Age International(P) Ltd, New Delhi

Reference Books

1. Berger, J.O.(1985): Statistical Decision Theory and Bayesian Analysis, 2/e, Springer Verlag.
2. Robert C.P. and Casella, G.(2004): Monte Carlo Statistical Methods, 2/e, Springer Verlag.
3. DeGroot, M.H.(2004): Optimal Statistical Decisions, Wiley-InterScience.
4. Gamerman, D. and Lobes H.F. (2000): Stochastic Simulation for Bayesian Inference, Taylor and Francis.
5. Box, G.P. and Tiao, G.C.(1973): Bayesian Inference in Statistical Analysis, Addison – Wesley.

Course Objectives:

1. To Know about various descriptions, characteristics, related random processes and background themes of *Poisson Queuing Models with single server*, and *multiple server*. To study the assumptions and derivations of different mathematical relations like steady state equations, Queue characteristics of Non Poisson (Erlangian) Queuing Models.
2. To Study the fundamental notions, applications and scope of Probabilistic and Deterministic Inventory Models. To describe and derive different mathematical relations of different Inventory models along with price break inventory policies.

Course Outcomes:

1. Derivation of and problem solving characteristics on (M/M/1): (∞ /FIFO) and (M/M/1): (N/FIFO) Models, simple numerical problems. Derivations and problem solving of steady state equations for different processes such as birth, death, migrations and Poisson, M/M/1 and M/M/C models.
2. Derivation and problem solving of different properties of Earlangian Queuing Models $M/E_k/1$, $E_k/M/1$ and $E_k/E_k/1$ models. Derivations and problem solving of EOQ, Optimal Total Cost, Optimal number of runs and optimal ordering times in deterministic inventory models with and without shortages. Understanding the notion of Inventory with Price breaks and optimal total cost and optimal order quantity with multiple price breaks.

Unit I

Poisson Queuing Models with single server: Descriptions of queuing models, Generalized Birth and Death Processes, steady state Birth and death processes- Assumptions, Probability distributions for number of Units (steady state), waiting time distribution, Derivation of characteristics on (M/M/1): (∞ /FIFO) and (M/M/1): (N/FIFO) Models, simple numerical problems

Unit II

Poisson Queuing Models with multiple server: Descriptions of the model, Assumptions, Probability distributions for number of Units (steady state), waiting time distribution, Derivation of characteristics on (M/M/C): (∞ /FIFO), (M/M/C): (N/FIFO) and (M/M/C): (C/FIFO) Models, simple numerical problems

Unit III

Non Poisson Queuing Models (Erlangian): Descriptions of the model, Assumptions, Probability distributions for number of Units (steady state), waiting time distribution, Derivation of characteristics on (M/ E_k /1), (E_k /M/1), simple numerical problems

UNIT – IV

Scope and notion of Inventory, Terminology, overview on probabilistic& Deterministic Models, optimality issues with Inventory; Deterministic Inventory models with shortages and without shortage. Finding EOQ and other characteristics, Simple Problem

UNIT – V

Deterministic Inventory models with simultaneous replenishment and stock clearance, with shortages and without shortages, finding EOQ and other parameters, Simple Numerical Problems; Deterministic Inventory models with Single and multiple price Breaks and numerical examples.

Books for Study:

1. KantiSwarup et al.:Operations Research, Sultan Chand and Sons,New Delhi
2. S.D Sharma: Operations Research
3. Donald Gross & Carl M Harris (1998): Fundamentals of Queuing theory, John Wiley & Sons, Inc.

4. Hamdy A.Taha(2006): Operations Research – An Introduction, 8/e , Prentice Hall of India Private Ltd., New Delhi

Books for Reference:

1. Hiller F S and Libermann G J (1995):Introduction to operations Reseach, 6th Edition, McGraw Hill
2. Prabhu N.U. (1965) Applied Stochastic Processes, Mc.Millan
3. J.Medhi (2009), Stochastic Processes, 3/e, New Age International
4. Bhat. B.R. (2002), Stochastic Processes, 2/e, New Age International

Course Objectives: This course is intended to equip students to get knowledge in clustering and classification techniques.

Course Outcomes: Students will gain knowledge on the working principle of algorithms related to clustering and classification techniques and its application to real life problems.

Unit I

Introduction to data mining – data types – Measures of similarity and dissimilarity – Data mining tools – supervised and unsupervised learning – Introduction to Cluster Analysis – Types of clustering – Agglomerative Hierarchical clustering algorithm – Issues – strength and weaknesses.

Unit II

Basic k-means algorithm – Issues – fuzzy clustering – fuzzy c means algorithm - cluster evaluation – unsupervised and supervised measures - Introduction to classification – Decision Trees – Building a decision tree – Tree induction algorithm – model over fitting – Evaluating the performance of a classifier

Unit III

Nearest Neighbor classifiers – kNN algorithm – Naïve Bayesian classifier – Binary logistic regression – odds ratio – Interpreting logistic regression coefficients – Multiple logistic regression

Unit IV

Association rules mining – Basics – Apriori algorithm – Pruning and candidate generation – Rule mining.

Unit V

Case studies based on k means clustering - fuzzy c means clustering - kNN classification - Binary logistic regression using R programming language.

Text Books

1. Tan, T., Steinbach, M. and Kumar, V. (2006): Introduction to Data Mining, Pearson Education. (relevant portions of Chapters 1, 2, 4, 5 and 8).
2. Gupta, G.K. (2008): Introduction to Data Mining with case studies, Prentice – Hall of India Pvt. Ltd. (relevant portions of Chapter 2)
3. Daniel T. Larose (2006): Data Mining: Methods and Models, John Wiley and sons. (relevant portions of Chapter 4).

Reference Books

1. Han, J. and Kamber, M. (2006): Data Mining: Concepts and Techniques, 2nd Edition, Morgan Kaufmann Publishers.
2. Paolo Giudici (2003): Applied Data Mining: Statistical Methods for Business and Industry, John Wiley and sons.
3. Rajan Chattamvelli (2009): Data Mining Methods, Narosa Publishing House, New Delhi.

SEMESTER IV

STAT 541 - PROJECT WORK & COMPREHENSIVE VIVA

CREDITS: 12

Course Objectives: This course is intended to expose students to apply the methodologies that were covered in the curriculum.

Course Outcomes: Students will gain knowledge on the working principle of advanced multivariate tools and techniques and their application to real life problems.

1. It is an individual project work offered in IV semester with 12 credits.
2. The Project work shall be guided and supervised by a faculty member assigned in the beginning of the semester.
3. The project work should be undertaken in a reputed and relevant organization and topics are to be selected in such a way that there is enough scope to apply and demonstrate the statistical techniques learnt in the course.
4. At the end of the semester, before the last working day, project report should be submitted (two copies) with a certificate from industrial guide.
5. The project report shall contain the statement of problem, Methodology adopted, statistical tools used for analysis, findings, conclusions, suggestions and references.
6. The project work will be assessed for 12 credits. Students have to give a seminar of their project report at the end of the semester and which will be evaluated internally.
7. There will be viva-voce examination by an internal and an external examiner during end semester examination in 4th semester.
8. Report shall have the following format: Chapter I for Introduction for providing conceptual clarity, Chapter II for Review of Literature, Chapter III for Methodology, Chapter IV, V & VI for analysis and interpretations of each objectives (Number of chapter can be reduced or increased depending upon the number of objectives), chapter VII for findings and suggestions.

Unit I

Basic deterministic model: Cash flows, discount function, interest and discount rates, balances and reserves, internal rate of return, The life table: Basic definitions, probabilities, construction of life tables, life expectancy, Life annuities: Introduction, calculating annuity premium, interest and survivorship discount function, guaranteed payments, deferred annuities.

Unit II

Life insurance: Introduction, calculation of life insurance premiums, types of life insurance, combined benefits, insurances viewed as annuities, Insurance and annuity reserves: The general pattern reserves, recursion, detailed analysis of an insurance, bases for reserves, non forfeiture values, policies involving a return of the reserve, premium difference and paid-up formula.

Unit III

Fractional durations: Life annuities paid monthly, immediate annuities, fractional period premium and reserves, reserves at fractional durations, Continuous payments: Continuous annuities, force of discount, force of mortality, Insurance payable at the moment of death, premiums and reserves. The general insurance – annuity identity, Select morality: Select an ultimate tables, Changed in formulas.

Unit IV

Multiple life contracts: Joint life status, joint annuities and insurances, last survivor annuities and insurances, moment of death insurances. The general two life annuity and insurance contracts, contingent insurances

Unit V

Multiple decrement theory: Basic model, insurances, Determination of the models from the forces of decrement. Stochastic approach to insurance and annuities; Stochastic approach to insurance and annuity benefits, deferred contracts, Stochastic approach to reserves and premiums, variance formula.

Text Books

1. Promislow, S.D(2006): Fundamentals of Actuarial Mathematics, John Willey, Chapters 2- 11 &14.
2. Newton L. Bowers, Jr, Hans U. Gerber, James C. Hickmann, Donald A. Jones and Cecil J. Nesbitt (1997): Actuarial Mathematics, The Society of Actuaries.

Reference Books

1. Neill, A. (1977): Life contingencies, Heinemann, London.
2. King, G. Institute of Actuaries Text Book. Part 11, Second edition, Charles and Edwin Layton, London.
3. Donald D.W.A. (1970): Compound Interest and Annuities, Heinemann, London.
4. Jordan, C.W. Jr. (1967): Life Contingencies, Second edition, Chicago Society of Actuaries.
5. Hooker, P.F. and Longley Cook, L.W. (1953): Life and other Contingencies, Volume I and Volume II (1957) Cambridge University Press.
6. Spurgeon, E.T. (1972): Life Contingencies, Third edition, Cambridge University Press.

Unit – I

Basic of SPSS – Importing and Exporting of files – Recoding and Computing new variables – Visual Binning – Selection of cases – splitting and merging of files – multiple responses – Graphical plots: Box Plot, Scatter plot, Histogram, Bar and Pie charts.

Unit – II

Fitting of Curves: Parabola, cubic and exponential – correlation and regression: simple, multiple – Rank correlation – Variable Selection in Multiple Regression - Residual Analysis: model adequacy, detection of outliers and influence observations.

Unit – III

Testing of Hypotheses – two sample and paired samples t – test; F-test for two sample variances; Chi-square test for independence of attributes – One way and Two Way Analysis of Variance – Multiple Comparison tests : Tukey's test, Duncan's Multiple range test and Dunnett's test.

Unit – IV

Non-Parametric tests: One sample and Two sample Kolmogorov – Smirnov test, Kruskal – Wallis test, Friedman test, Median Test – One Way MANOVA – Hotelling's T^2 two sample test – Test for two Covariance matrices – One way Repeated Measures ANOVA.

Unit - V

Factor Analysis : Identification of Principle Component, Varimax rotation – Discriminant Analysis – Enter and Stepwise procedures, discriminant scores – Logistic regression – variable selection procedures (Backward and Forward with conditional and wald methods), Odds ratio, Classification matrix – 2^2 , 2^3 , 3^2 and 3^3 factorial designs – Split Plot designs.

Books for Study

1. Ajai S. Gaur and Sanjaya S Gaur (2009), Statistical Methods for Practice and Research - A Guide to Data Analysis Using SPSS, Second Edition, SAGE Publications Pvt. Ltd
2. William E Wagner, III (2010), Using IBM® SPSS® Statistics for Social Statistics and Research Methods, Third Edition, PINE FORGE PRESS, An Imprint of SAGE
3. Robert Ho (2006), Handbook of Univariate and Multivariate Data Analysis and Interpretation with SPSS, Chapman and Hall, CRC Press

Books for Reference

1. Sarma KVS (2010), Statistics Made Simple – Do It Yourself on PC, Second Edition, PHI Learning.
2. Sabina Landau and Brian S. Everitt (2004), A Handbook of Statistical Analysis using SPSS, Chapman and Hall, CRC Press
3. Andy Field (2009), Discovering Statistics Using SPSS (Introducing Statistical Methods Series), Third Edition, SAGE Publications Ltd.

Course Objectives: This course is intended to provide basics of demography and official statistics

Course Outcomes: Students will gain knowledge about constructions of life tables and measures of population dynamics.

Unit I

Sources of demographic Statistics, Basic demographic measures: Ratios, Proportions and percentages, Population Pyramids, Sex ratio Crude rates, Labour force participation rates, Density of population, Probability of dying.

Unit II

Life tables: Construction of a life table, Graphs of l_x , q_x , d_x , Functions L_x , T_x , and E_x . Abridged life tables Mortality: Rates and Ratios, Infant mortality, Maternal mortality, Expected number of deaths, Direct and Indirect Standardization, Compound analysis, Morbidity.

Unit III

Fertility: Measures of Fertility, Reproductively formulae, Rates of natural increase, Fertility Schedules, Differential fertility, Stable Populations, Calculation of the age distribution of a stable population, Model Stable Populations.

Unit IV

Population estimates, Population Projections: Component method, Mortality basis for projections, Fertility basis for projections, Migration basis for projections.

Unit V

Ageing of the population, Estimation of demographic measures from incomplete data.

Text Books:

1. Pollard, A. H. Yusuf, F. and Pollard, G.N. (1990). Demographic Techniques, Pergamon Press, Chapters 1-8, 12.

Reference Books:

1. Keyfitz, N. (1977) Applied Mathematical Demography A Willey-Interscience Publication.
2. Keyfilz, N. (1968) Introduction to the Mathematic of Population Ready, Mass: Addition-Wesley.
3. Keyfilz, N. and Caswell, H. (2005) Applied Mathematical Demography, Third edition, Springer.

Course Objectives:

Providing a clear explanation of the fundamental theory of time series analysis and forecasting with regression and autoregression combination models. Modeling and forecast evaluation, along with a sample size analysis for common time series models to attain adequate statistical power.

Course outcomes :

The students who have studied this course are able to read and retrieve the real time data and work with it efficiently and effectively with the help of packages like R and Python, students are trained in identifying the data and models which will suit the data.

Unit I

Exploratory Time Series Analysis: Forecasting trend and seasonality based on smoothing. Methods of Exponential and moving average smoothing; Types and implications of interventions; Outliers, additive and innovational outliers, procedure for detecting outliers

Unit II

Stationary Stochastic models: weak and strong stationarity, Deseasonalising and detrending an observed time series, Auto-covariance, autocorrelation function (ACF), partial autocorrelation function (PACF) and their properties, Conditions for stationarity and invertibility,

Unit III

Models for Time Series: Time series data, Trend, seasonality, cycles and residuals, Stationary, White noise processes, Autoregressive (AR), Moving Average (MA), Autoregressive and Moving Average (ARMA) and Autoregressive Integrated Moving Average (ARIMA) processes, Choice of AR and MA periods

Unit IV

Spectral analysis and decomposition: Spectral analysis of weakly stationary process, Periodogram and Correlogram analysis, Spectral decomposition of weakly AR process and representation as a one-sided MA process – necessary and sufficient conditions, implication in prediction problems.

Unit V

Modeling Seasonal Time Series: seasonal ARIMA models, estimation and forecasting, Fitting ARIMA models with Box-Jenkins procedure, Identification, Estimation, Verification, Test for white noise, Forecasting with ARMA models.

Text Books:

1. Nicholas T. Thomopoulos, 1980, Applied Forecasting Methods, Prentice Hall
2. BoxGEP, JenkinsGM and ReinselGC (2004): Time Series Analysis–Forecasting and Control, Pearson Education.
3. BrockwellPJ and DavisRA (2002): Introduction to Time Series and Forecasting, Springer.
4. Montgomery D C and Johnson L A (1977): Forecasting and Time Series analysis, McGraw Hill.

Reference Books:

1. ChatfieldC (1996): The Analysis of Time Series: Theory and Practice, fifth edition, Chapman and Hall.
2. Nachane D.M. (2006): Econometrics: Theoretical Foundations and Empirical Perspective, Oxford University Press
3. Diggle, P.J Time Series: A Bio-statistical Introduction, Oxford University Press

(1990).

4. Hamilton, J., 1994, Times Series Analysis, Princeton University Press.
5. Harvey, A.C., 1993, Time Series Models, MIT Press.
6. Kendall, Sir Maurice and Ord J K (1990): Time Series, Edward Arnold.
7. Tsay, R., 2002, Analysis of Financial Time Series, Wiley Series

Course Objectives: To give exposure on the practical implementation of the quality control techniques and acceptance sampling schemes.

Course Outcomes: Students will be able to cater the needs of the industry to resolve the quality issues.

Unit I

Need for TQM, evolution of quality, Definition of quality, TQM philosophy – Contributions of Deming, Juran, Crosby, Taguchi and Ishikawa.

Unit II

Vision, Mission, Quality policy and objective, Planning and Organization for quality, Quality policy Deployment, Quality function deployment, Analysis of Quality Costs.

Unit III

Customer focus, Leadership and Top management commitment, Employee involvement – Empowerment and Team work, Supplier Quality Management, Continuous process improvement, Training, performance Measurement and customer satisfaction.

Unit IV

PDSA, The Seven QC Tools of Quality, New Seven management tools, Concept of six sigma, FMEA, Bench Marking, JIT, POKA YOKE, 5S, KAIZEN, Quality circles.

Unit V

Need for ISO 9000 Systems, clauses, Documentation, Implementation, Introduction to QS 9000, Implementation of QMS, Case Studies.

Text Books

1. Dale H. Besterfield (2002): "Total Quality Management", Pearson Education Asia
2. Oakland, J.S. (1989): "Total Quality Management", Butterworth-Heinemann Ltd., Oxford

Reference Books

1. Narayana V. and Sreenivasan, N.S. (1996): "Quality Management – Concepts and Tasks", New Age International.
2. Zeiri (1991): "Total Quality Management for Engineers", Wood Head Publishers.
3. Juran J.M and Frank M. Gryna Jr. (1982): "Quality Planning and Analysis", TMH, India.
4. Brain Rethery (1993): ISO 9000, Productivity and Quality Publishing Pvt. Ltd.
5. D. Mills (1993): Quality Auditing, Chapman and Hall.

SOFT CORE COURSE FOR OTHER DEPARTMENTS

STAT 418 STATISTICAL METHODS

Credits: 3

Course Objectives: To focus attention on various statistical methods and to apply them for basic data analysis.

Course Outcome: Students will be able to present the data in terms of graphs, summary statistics and comparative analysis.

Unit I

Definition of statistics – Scope and limitations of statistics – Primary and Secondary data and its sources - Simple Random, Stratified and Systematic sampling techniques - preparation of a questionnaire -Collection and classification of data – Frequency tables – Diagrammatic and Graphical representation of data

Unit II

Measures of central tendency – Mean, Median and Mode – Measures of dispersion – Range, Quartile deviation and Standard deviation – Coefficient of variation and skewness

Unit III

Study of relationship between variables: Quantitative: Correlation and Regression – Partial and Multiple correlation (three variables only) – Qualitative: Contingency tables – Measures of Association.

Unit IV

Elementary Probability theory: Addition theorem – Conditional probability and Multiplication theorem - Baye's Theorem – Random variables and probability distributions – Binomial, Poisson , Normal (simple applications of the distribution) – Sampling distributions: t, F and chi-square (definition only)

Unit V

Hypothesis testing: Basic concepts in Hypothesis Testing – Types of error – Tests for Mean and Proportion based on Normal and Student t-distribution - Chi-square test for independence of attributes – One-way and two-way Analysis of Variance

Text Books

1. Hooda.R.P.(2003) : Statistics for Business and Economics , 3/e, Mac Millan .
2. Medhi.J. (1992) : Statistical Methods an Introductory Text , Wiley Eastern Ltd.,.
3. Kapoor.V.K. and Gupta.S. (1978): Fundamentals of Applied Statistics,Sultan Chand and Sons.
4. Sharma J.K.(2004): Business Statistics, Pearson Education

Reference Books

1. Agarwal.B.L(1996): Basic statistics, 3/e, New Age International (P) Ltd.,.
2. Anderson.R, Sweeney.J and Williams.A (2002): Statistics for Business and Economics, 8/e, Thomson.
3. Sheldon M.Ross (2006): Introductory Statistics, 2/e, Elsevier Publications.
4. Murray R. Spiegel and Larry J. Stephens (2005): Schaum's Outline of Theory and Problems of Statistics, 3/e, Tata Mc Graw Hill Publishing Company Ltd, New Delhi.